



Formalni upitni jezici

Baze podataka 1

dr Miloš CVETANOVIĆ



- Proceduralni jezici
 - **Relaciona algebra**
- Deklarativni jezici
 - Relacioni račun domena
 - Relacioni račun n-torki



Biblioteka

OBLAST (SifO, Naziv)

NASLOV (SifN, Naziv)

KNJIGA (SifK, SifN)

CLAN (SifC, Ime)

POZAJMICA (SifP, SifC, SifK, SifN, Datum, Dana)

REZERVACIJA (SifC, SifN, DatumVreme)

DRZI (SifK, SifC, Datum)

JE_REZERVISANA (SifK, SifC, Datum)



Restrikcija

- Struktura relacije se ne menja
- Kardinalnost $N(t) \leq N(r)$
- Primer 1
 $\sigma_{\text{SifO}=\text{"PJ"}}(\text{naslov}) \rightarrow t(\text{SifN}, \text{Naziv}, \text{SifO})$
- Primer 2
 $\sigma_{\text{Koji} > 1}(\text{je_autor}) \rightarrow t(\text{SifA}, \text{SifN}, \text{Koji})$



Projekcija

- Struktura relacije se menja
- Kardinalnost $N(t) \leq N(r)$
- Primer 1
 $\pi_{\text{Naziv, SifO}}(\text{naslov}) \rightarrow t(\text{Naziv, SifO})$
- Primer 2
 $\pi_{\text{Naziv}}(\sigma_{\text{SifO}=\text{"PJ"}}(\text{naslov})) \rightarrow t(\text{Naziv})$



Unija

- Unijska kompatibilnost
 - Šeme relacija imaju isti broj atributa
 - Atributi šema relacija redom odgovaraju jedni drugima (**po tipu i značenju**)
- Kardinalnost: $\max(N(r), N(s)) \leq N(t) \leq N(r)+N(s)$
- Primer 1
clan U autor $\rightarrow t(\text{SifX}, \text{Ime})$
- Primer 2
 $\pi_{\text{SifK}}(\text{drzi}) \rightarrow t1(\text{SifK})$
 $\pi_{\text{SifK}}(\text{pozajmica}) \rightarrow t2(\text{SifK})$
 $t1 \cup t2 \rightarrow t3(\text{SifK})$



Razlika

- Unijska kompatibilnost
- Kardinalnost: $0 \leq N(t) \leq N(r)$
- Primer 1
$$\pi_{\text{SifC, SifK}}(\text{drzi}) \rightarrow t1(\text{SifC, SifK})$$
$$\pi_{\text{SifC, SifK}}(\text{pozajmica}) \rightarrow t2(\text{SifC, SifK})$$
$$t1 - t2 \rightarrow t3(\text{SifC, SifK})$$
- Primer 2
$$\pi_{\text{SifC}}(\text{clan}) \rightarrow t1(\text{SifC})$$
$$\pi_{\text{SifC}}(\text{drzi}) \rightarrow t2(\text{SifC})$$
$$t1 - t2 \rightarrow t3(\text{SifC})$$
- $\pi_{\text{SifC}}(\text{clan}) - \pi_{\text{SifC}}(\text{drzi}) \rightarrow t3(\text{SifC})$



Presek

- Unijska kompatibilnost
- Kardinalnost: $0 \leq N(t) \leq \min(N(r), N(s))$
- Ekvivalentno sa: $r - (r - s)$



Dekartov proizvod

- Šema rezultatne relacije sadrži sve atribute polaznih relacija
- Kardinalnost: $N(t) = N(r) * N(s)$



Spajanje

$$r \times_{P(XY)} s = \sigma_{P(XY)}(r \times s) = t(XY) = \{xy \mid x \in r \wedge y \in s \wedge P(xy)\}$$

$$(r \times_{X_i \Theta Y_k} s); \Theta \in \{=, \leq, \geq, <, >, \neq\}; X_i \in X; Y_k \in Y;$$

$$(r \times_{X=Y} s); X = (X_1, \dots, X_n); Y = (Y_1, \dots, Y_n); X_1 = Y_1 \wedge X_2 = Y_2 \dots;$$

$$(r \times_{A*B} s); A = B; A \subseteq X, B \subseteq Y; \pi_{XY-B}(\sigma_{A=B}(r \times s)) = t(XY - B)$$



Deljenje

- $\pi_{\text{SifA}, \text{SifN}}(\text{je_autor}) \rightarrow \text{t1}(\text{SifA}, \text{SifN})$
- $\pi_{\text{SifN}}(\sigma_{\text{SiFO}=\text{"PJ"}}(\text{naslov})) \rightarrow \text{t2}(\text{SifN})$

autor-naslov (r)

naslov-pj (s)

- $\pi_{\text{SifA}}(\text{je_autor}) \rightarrow \text{t3}(\text{SifA})$
- $\text{t3} \times \text{t2} \rightarrow \text{t4}$
- $\text{t4} - \text{t1} \rightarrow \text{t5}$
- $\text{t3} - \pi_{\text{SifA}}(\text{t5}) \rightarrow \text{t6}$

autor-sif ($\pi_x(r)$)

svi-sve ($\pi_x(r) \times s$)

nije-autor (($\pi_x(r) \times s$)-r)

trazene-sif



Primer A

- $\pi_{\text{SifC}}(\text{drzi}) \rightarrow \text{drz}(\text{SifC})$
- $\pi_{\text{SifC}}(\text{pozajmica}) \rightarrow \text{poz}(\text{SifC})$
- $\text{drz} \cup \text{poz} \rightarrow \text{drzpoz}(\text{SifC})$
- $\text{clan } x * \text{drzpoz} \rightarrow \text{svedrzpoz}(\text{SifC}, \text{lme})$
- $\pi_{\text{lme}}(\text{svedrzpoz}) \rightarrow \text{resenje}(\text{lme})$

- $\pi_{\text{lme}}(\text{clan } x * (\pi_{\text{SifC}}(\text{drzi}) \cup \pi_{\text{SifC}}(\text{pozajmica})))$

- Davati smisljena imena relacijam koje nastaju kao međurezultat
- Komentarisati značenje međurezultata
- Navoditi koje attribute sadrže relacije međurezultata



Primer B

- $\pi_{\text{SifC}, \text{SifK}}(\text{drzi}) \cup \pi_{\text{SifC}, \text{SifK}}(\text{pozajmica}) \rightarrow t1(\text{SifC}, \text{SifK})$
- $\pi_{\text{SifC}, \text{SifN}}(\text{knjiga } x * t1) \rightarrow t2(\text{SifC}, \text{SifN})$
- $\pi_{\text{SifN}}(\sigma_{\text{SifO}=\text{"PJ"}}(\text{naslov})) \rightarrow t3(\text{SifN})$
- $t2 / t3 \rightarrow t4(\text{SifC})$
- $\pi_{\text{SifN}}(\sigma_{\text{SifO}=\text{"BP"}}(\text{naslov})) \rightarrow t5(\text{SifN})$
- $\pi_{\text{SifK}}(\text{knjiga } x * t5) \rightarrow t6(\text{SifK})$
- $t1 \times t6 \rightarrow t7(\text{SifC}, \text{SifK})$
- $t4 - \pi_{\text{SifC}}(t7) \rightarrow t8(\text{SifC})$
- $\pi_{\text{Ime}}(\text{clan } x * t8) \rightarrow \text{resenje}(\text{Ime})$



Primer C

- Data je šema relacione baze podataka

FILM(SifF, Naziv, Duzina, Ocena, Cena, SifZ);

KASETA(SifK, Duzina);

ZANR(SifZ, Naziv);

POZAJMICA(SifP, SifK, SifF, SifC, Dana);

SADRZI(SifK, SifF);

CLAN(SifC, Ime, Popust);

- Sastaviti iskaze relacione algebre koji daju šifre i nazive filmova koji su sadržani na jednoj ili više kaseti a nisu pozajmljivani.
- Sastaviti iskaze relacione algebre koji daju šifre i imena članova koji su pozajmili bar jedan od filmova koji imaju najmanju ocenu među filmovima svog žanra.



Dodatni operatori relacione algebre

- Preimenovanje

$$\rho_{s(A_1, A_2, \dots, A_n)}(r) \rightarrow s(A_1, A_2, \dots, A_n)$$

- Agregatne operacije

$$G_1, G_2, \dots, G_n \quad \mathcal{G}_{F_1(A_1), F_2(A_2), \dots, F_n(A_n)}(r)$$

G_i – atributi po kojima se grupiše

F_i – agregatna operacija

{sum, avg, max, min, count, count-distinct}

A_i – atributi relacije



- Proceduralni jezici
 - Relaciona algebra
- Deklarativni jezici
 - **Relacioni račun domena**
 - Relacioni račun n-torki



Relacioni račun domena – primeri 1

$$\{ \langle SifN, Naziv, SifO \rangle \mid \langle SifN, Naziv, SifO \rangle \in naslov \wedge SifO = "PJ" \}$$

$$\{ \langle Naziv, SifO \rangle \mid \exists SifN (\langle SifN, Naziv, SifO \rangle \in naslov) \}$$

$$\{ \langle SifX, IME \rangle \mid \exists SifA (\langle SifA, IME \rangle \in autor \wedge SifA = SifX) \vee \\ \vee \exists SifC (\langle SifC, IME \rangle \in clan \wedge SifC = SifX) \}$$

$$\{ \langle SifC \rangle \mid \exists IME (\langle SifC, IME \rangle \in clan) \wedge \\ \wedge \neg \exists SifK, Datum (\langle SifK, SifC, Datum \rangle \in drzi) \}$$



Relacioni račun domena – primeri 2

$$\{ \langle SifK \rangle \mid \exists SifC, Datum(\langle SifK, SifC, Datum \rangle \in drzi) \vee \\ \vee \exists SifP, SifC, SifN, Dana(\langle SifP, SifC, SifK, SifN, Dana \rangle \in pozajmica) \}$$

$$\{ \langle SifC, SifK \rangle \mid \exists Datum(\langle SifK, SifC, Datum \rangle \in drzi \wedge \\ \wedge \exists SifP, SifN, Dana(\langle SifP, SifC, SifK, SifN, Dana \rangle \in pozajmica)) \}$$

$$\{ \langle SifN, NazivN, SifON, SifO, NazivO \rangle \mid \langle SifN, NazivN, SifON \rangle \in naslov \wedge \\ \wedge \langle SifO, NazivO \rangle \in oblast \wedge SifON = SifO \}$$

$$\{ \langle SifN, Naziv, NazivO \rangle \mid \exists SifON((\langle SifN, Naziv, SifON \rangle \in naslov) \wedge \\ \wedge \exists SifO(\langle SifO, NazivO \rangle \in oblast \wedge SifO = SifON)) \}$$



Relacioni račun domena – primeri 3

$$\{ \langle IME \rangle \mid \exists SifC (\langle SifC, IME \rangle \in \text{clan} \wedge \\ \wedge (\exists SifK, Datum (\langle SifK, SifC, Datum \rangle \in \text{drzi}) \vee \\ \vee \exists SifP, SifK_1, SifN, Dana (\langle SifP, SifC, SifK_1, SifN, Dana \rangle \in \text{pozajmica}))) \}$$
$$\{ \langle IME \rangle \mid \exists SifA (\langle SifA, IME \rangle \in \text{autor} \wedge \\ \wedge \exists SifN, Naziv, SifO (\langle SifN, Naziv, SifO \rangle \in \text{naslov} \wedge \\ \wedge SifO = "PJ" \wedge \exists Koji (\langle SifA, SifN, Koji \rangle \in \text{je_autor}))) \}$$
$$\{ \langle SifN \rangle \mid \exists SifC, Datum (\langle SifN, SifC, Datum \rangle \in \text{rezervacija}) \wedge \\ \wedge \exists SifK (\langle SifK, SifN \rangle \in \text{knjiga} \wedge \\ \wedge \neg \exists SifC, Datum (\langle SifK, SifC, Datum \rangle \in \text{drzi})) \}$$



- Proceduralni jezici
 - Relaciona algebra
- Deklarativni jezici
 - Relacioni račun domena
 - **Relacioni račun n-torki**



Relacioni račun n-torki – primeri 1

$$\{t \mid t \in \textit{naslov} \wedge t[\textit{SifO}] = \textit{"PJ"}\}$$

$$\{t \mid \exists u(u \in \textit{naslov} \wedge t[\textit{Naziv}] = u[\textit{Naziv}] \wedge t[\textit{SifO}] = u[\textit{SifO}])\}$$

$$\{t \mid \exists u(u \in \textit{autor} \wedge t[\textit{SifX}] = u[\textit{SifA}] \wedge t[\textit{IME}] = u[\textit{IME}]) \vee \\ \vee \exists u(u \in \textit{clan} \wedge t[\textit{SifX}] = u[\textit{SifC}] \wedge t[\textit{IME}] = u[\textit{IME}])\}$$

$$\{t \mid \exists u(u \in \textit{clan} \wedge t[\textit{SifC}] = u[\textit{SifC}] \wedge \neg \exists v(v \in \textit{drzi} \wedge u[\textit{SifC}] = v[\textit{SifC}]))\}$$



Relacioni račun n-torki – primeri 2

$$\{t \mid \exists u(u \in drzi \wedge t[SifK] = u[SifK]) \vee \exists u(u \in pozajmica \wedge t[SifK] = u[SifK])\}$$

$$\{t \mid \exists u(u \in drzi \wedge t[SifC] = u[SifC] \wedge t[SifK] = u[SifK] \wedge \\ \wedge \exists v(v \in pozajmica \wedge u[SifC] = v[SifC] \wedge u[SifK] = v[SifK]))\}$$

$$\{t \mid \exists u(u \in naslov \wedge t[SifN] = u[SifN] \wedge t[NazivN] = u[Naziv] \wedge t[SifON] = u[SifO] \wedge \\ \wedge \exists v(v \in oblast \wedge t[SifO] = v[SifO] \wedge t[NazivO] = v[Naziv] \wedge u[SifO] = v[SifO]))\}$$

$$\{t \mid \exists u \in naslov \wedge t[SifN] = u[SifN] \wedge t[NazivN] = u[Naziv] \wedge \\ \wedge \exists v(v \in oblast \wedge t[NazivO] = v[Naziv] \wedge u[SifO] = v[SifO]))\}$$



Relacioni račun n-torki – primeri 3

$$\{t \mid \exists u(u \in \text{clan} \wedge t[\text{IME}] = u[\text{IME}] \wedge \\ \wedge (\exists v(v \in \text{drzi} \wedge u[\text{SifC}] = v[\text{SifC}]) \vee \\ \vee \exists v(v \in \text{pozajmica} \wedge u[\text{SifC}] = v[\text{SifC}]))))\}$$

$$\{t \mid \exists u(u \in \text{autor} \wedge t[\text{IME}] = u[\text{IME}] \wedge \\ \wedge \exists v(v \in \text{naslov} \wedge v[\text{SifO}] = \text{"PJ"} \wedge \\ \wedge \exists x(x \in \text{je_autor} \wedge v[\text{SifN}] = x[\text{SifN}] \wedge u[\text{SifA}] = x[\text{SifA}]))))\}$$

$$\{t \mid \exists u(u \in \text{rezervacija} \wedge t[\text{SifN}] = u[\text{SifN}] \wedge \\ \wedge \exists v(v \in \text{knjiga} \wedge u[\text{SifN}] = v[\text{SifN}] \wedge \\ \wedge \neg \exists x(x \in \text{drzi} \wedge v[\text{SifK}] = x[\text{SifK}]))))\}$$